

2D Shapes	
Area of Triangle	$\frac{1}{2} \times \text{base} \times \text{height}$
Area of Parallelogram	base \times height
Area of Rectangle	$l \times w$
Area of Trapezoid	$\frac{1}{2} \times (\text{sum of parallel sides}) \times \text{height}$
Circumference & Area: Circle	$c = 2\pi r, A = \pi r^2$
Length of an arc	$\frac{\theta}{360} \times 2\pi r$
Area of a Sector	$\frac{\theta}{360} \times \pi r^2$

3D Shapes	
Cuboid Surface area	$SA = 2xy + 2xz + 2yz$ where x, y, z are side lengths
Cuboid Volume	$V = xyz$ where x, y, z are side lengths
Cylinder Surface Area	$SA = 2\pi rh + 2\pi r^2$ Note: Curved part: $2\pi rh$
Cylinder Volume	$V = \pi r^2 h$
Cone Surface Area	$SA = \pi r l + \pi r^2$ Note: Curved part: $\pi r l$, l is slant length
Cone Volume	$V = \frac{1}{3} \pi r^2 h$
Sphere Surface Area	$SA = 4\pi r^2$ Note: Hemisphere $3\pi r^2$
Sphere Volume	$v = \frac{4}{3} \pi r^3$ Note: Hemisphere $\frac{2}{3} \pi r^3$
Prism Volume	$V = \text{Area of cross section} \times \text{height}$
Pyramid Volume	$V = \frac{1}{3} \times \text{base area} \times h$

Indices	
Multiplication	$x^a \times x^b = x^{a+b}$ $(x^a)^b = x^{ab}$ $(cx^a)^b = c^b x^{ab}$
Division	$x^a \div x^b = x^{a-b}$
Negative Powers	$x^{-n} = \frac{1}{x^n}$
Fractions	$\left(\frac{x}{y}\right)^{-n} = \frac{y^n}{x^n}$ and $\left(\frac{x}{y}\right)^n = \frac{x^n}{y^n}$
Fractional Powers	$\frac{x}{a^m} = \frac{1}{\sqrt[m]{a^n}}$

Percentages	
One amount as a % of the other amount (wants answer as a %)	$\frac{a}{b} \times 100$ Look for the words as a percent of
Percentage gain/loss (wants answer as a %)	$\frac{\text{difference}}{\text{original}} \times 100$ Look for the words percentage gain/loss/increase/decrease
Find percentage of an amount	$\frac{\%}{100} \times \text{amount}$
Given % of an amount, find the full amount	$\frac{\text{given amount}}{\frac{\%}{100}}$
Increasing/decreasing by a %	$\text{amount} \left(1 \pm \frac{\%}{100}\right)$ + if increase - if decrease
Given % of an amount after amount has been added or subtracted, find the full amount	$\frac{\text{Amount}}{1 \pm \frac{\%}{100}}$ + if increase - if decrease Look for the words originally, at the beginning, before...

Pyramid Method For Percentages:

Cross off what you want and do the resulting operation (multiplication or division)
Note: we use the pyramid on the right if increasing/decreasing by an amount

Simple Interest (Interest on initial amount)	$\text{amount} + \left(\text{amount} \times \frac{\%}{100} \times \text{time}\right)$ $\text{Interest} = \text{amount} \times \frac{\%}{100} \times \text{time}$ Note: Make sure t and % are same unit of time
Compound Interest (Interest added also earns interest)	$FV = PV \left(1 + \frac{r}{100}\right)^t$ FV=future value, PV=present value t=time, r= interest rate

Quadratics	
Quadratic Function: Solutions to $ax^2 + bx + c = 0$	$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}, a \neq 0$
Completing The Square $ax^2 + bx + c = 0$	$a \left(x \pm \frac{b}{2a}\right)^2 + c - \frac{b^2}{4a}$
Max/Min Value	$C - \frac{b^2}{4a}$

Compound Measures	
Speed	$\text{speed} = \frac{\text{distance}}{\text{time}}$
Density	$\text{density} = \frac{\text{mass}}{\text{volume}}$
Pressure	$\text{pressure} = \frac{\text{force}}{\text{area}}$

Cross off what you want and do the resulting operation (multiplication or division)

Congruent Shapes	
SSS (side side side)	Three sides of each triangle equal
SAS (side angle side)	Two sides and included angle equal
AAS (angle angle side)	Two angles and corresponding side equal
RHS (right hypotenuse leg)	Contains right angle and hypotenuse and another side equal

Direct/Indirect Proportion y is... proportional to x
Directly: $y = kx$, Inversely: $y = \frac{k}{x}$

Statistics	
Frequency Density	Frequency density = $\frac{\text{frequency}}{\text{class width}}$
Pie chart	Angle = $\frac{\text{category frequency}}{\text{total}} \times 360$
Cumulative frequency	This is a running total of the frequencies
Box Plot	

Fractions/Decimals/Percentages	
Simplifying Fractions	Step 1: Find a factor of both numbers i.e. a number that fits in both the numerator AND denominator Step 2: Say how many times for each Step 3: Check whether you can do steps 1 and 2 again.
Fraction Of Amount	$\frac{2}{5}$ of amount Step 1: Divide amount by 5 Step 2: Multiply answer found by 2
Improper to Mixed	Step 1: Divide the numerator by the denominator Step 2: Write down the whole number answer to step 1 Step 3: Put the remainder in the numerator. The new denominator remains the same as that of the original improper fraction.
Mixed to Improper	Step 1: Multiply the whole number by the fraction's denominator Step 2: Add the numerator to step 1 and this is the new numerator Step 3: write the result: the top of the original denominator.
+ and - Fractions	Need a common denominator (the smallest number that that both the numerator and denominator fit into)
\times Fractions	Don't need common denominator. Can cancel diagonally or vertically, not horizontally.
\div Fractions	Don't need a common denominator. "Keep change flip"
Decimal to Fraction	Write over 10,100,1000 etc depending on how many places after the decimal and simplify.
Decimal to Percent	Multiply by 100
Fraction to Decimal	Write as an equivalent fraction over 10,100,1000 etc and then easy to divide by this number OR Use short division if can't write as an equivalent fraction
Fraction to Percent	Turn into a decimal and then just a decimal to percent question i.e. multiply decimal found by 100
Percent to Decimal	Divide by 100
Percent to Fraction	Write over 100 and simplify

Geometry	
Straight Line Equation	<ul style="list-style-type: none"> Slope intercept $y = mx + c$ General $ax + by + d = 0$ To get this form we put all the terms from form 1 on one side and multiply all terms by the denominators to get rid of the fractions (if we have them)
Straight Line Gradient/Slope Between 2 Points $(x_1, y_1), (x_2, y_2)$	$\text{slope} = \frac{y_2 - y_1}{x_2 - x_1}$ OR $\frac{\Delta y}{\Delta x}$ In English this formula just says: subtract the y coordinates and divide by the answer we get by subtracting the x coordinates. It doesn't matter which way round we subtract, just so long as we keep the same direction.
Coordinates of midpoint of 2 points $(x_1, y_1), (x_2, y_2)$	$\text{midpoint} = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$ In English this formula just says: Add the x coordinates and divide by 2 (i.e. find the average) and add the y coordinates and divide by 2 (i.e. find this average).
Distance Between 2 Points $(x_1, y_1), (x_2, y_2)$	$\text{distance} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$

Methods to find the equation of a straight line

$y = mx + c$
gradient/slope m , y intercept c

We use the letter m to represent slope and c to represent y intercept. If we can find the gradient m and y intercept c then we are done.

Step 1: Find the gradient m using one of the following 5 ways

- Way 1: If given a graph \Rightarrow pick any 2 points on the graph and use $\frac{\text{rise}}{\text{run}}$
- Way 2: If given a graph \Rightarrow pick any 2 points on the graph and use the slope formula
- Way 3: If given another line parallel to \Rightarrow locate m for this line and use same slope
- Way 4: If given another line perpendicular to \Rightarrow locate m for this line and don't use the same slope but instead "flip the fraction and change the sign" (this I just the fact that perpendicular slopes multiply to make -1.
 - If a line has slope 2 (note: this means the same as $\frac{2}{1}$) then a perpendicular slope is $-\frac{1}{2}$
 - If a line has slope $-\frac{1}{2}$ then a perpendicular slope is 2
 - If a line has slope 2 then a perpendicular slope is $-\frac{1}{2}$
- Way 5: If given 2 points \Rightarrow use formula $\frac{y_2 - y_1}{x_2 - x_1}$

$y = x - 1$ We can spot this straight away gradient = 2	$y = x + 2$ This means the same as $y = x + 2$ gradient = 1	$2x + 4y = 5$ We need to use algebra to re-arrange $4y = -2x + 5$ $y = \frac{-2x + 5}{4}$ This means the same as $y = -\frac{1}{2}x + \frac{5}{4}$ gradient = $-\frac{1}{2}$	$5x - 2y = 7$ We need to use algebra to re-arrange $-2y = -5x + 7$ $y = \frac{-5x + 7}{-2}$ We can split this up in order to separate the gradient and y intercept $y = \frac{5}{2}x - \frac{7}{2}$ gradient = $\frac{5}{2}$	$x + 2y = 8$ We need to use algebra to re-arrange $2y = -x - 5$ $y = \frac{-x - 5}{2}$ We can split this up in order to separate the gradient and y intercept $y = -\frac{1}{2}x - \frac{5}{2}$ gradient = $-\frac{1}{2}$
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Step 2: Find the y intercept c using one of the following 2 ways

- Way 1: read it off the graph (if given graph this is where the graph crosses the y axis)
- Way 2: plug the point given (x, y) into the equation (replace x with the x value and y with the y value).

$y = mx + c$

Make sure the slope m from step 1 is plugged in and solve/re-arrange for c using algebra. Make sure you plug in the point that the line passes through, not just any point.

Right Angled Trigonometry	
Pythagoras	$a^2 + b^2 = c^2$ if given hyp \Rightarrow subtract, if finding hyp \Rightarrow add
SOHCAHTOA	$\sin x^\circ = \frac{\text{opp}}{\text{hyp}}, \cos x^\circ = \frac{\text{adj}}{\text{hyp}}, \tan x^\circ = \frac{\text{opp}}{\text{adj}}$
Exact Trig Values	

Non Right-Angled Trigonometry	
Sine Rule	Finding a side: $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$ Finding an angle: $\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$
Cosine Rule	Finding a side: $a^2 = b^2 + c^2 - 2bc \cos A$ Finding an angle: $A = \cos^{-1} \left(\frac{b^2 + c^2 - a^2}{2bc}\right)$
Area of Triangle	$\frac{1}{2} ab \sin C$

Functions	
Inverse	Replace $f(x)$ with y , swap x & y , solve for y
Composite	$f(g(x))$ means plug $g(x)$ into $f(x)$
Transformations	$a f(bx + c) + d$ "anything in a bracket affects x and does the opposite" a=vertical stretch of a , b=horizontal stretch of $\frac{1}{b}$ c=translation c units in x direction d=translation d units in y direction $f(-x)$ =refl in x axis $-f(x)$ =refl in y axis

Circle Theorems

Angle at the centre is double the angle at the circumference

Angles subtended in the same segment by a chord are equal

Angle in a semicircle is a right angle

Tangents which meet at a point are equal in length

Opposite angles of a cyclic quadrilateral add to 180°

Alternate segment theorem: The angle between a tangent and a side of a triangle is equal to the opposite angle

Extra helpful facts to remember

- Angles in a triangle add to 180°
- Angles in a quadrilateral add to 360°
- Angles in a circle add to 360°
- Angles in a straight line add to 180°
- Angles at a point add to 360°
- Angles in the same segment are equal
- Angles in the same segment are equal
- Angles in the same segment are equal
- Angles in the same segment are equal

For two intersecting chords, the products of their diagonals are equal

 $ab = cd$
 $a(a + b) = c(c + d)$

Series (IGCSE only)	
Arithmetic sequence:	n th term: $u_n = a + (n - 1)d$ sum of n terms: $S_n = \frac{n}{2} [2a + (n - 1)d] = \frac{n}{2} (a + l)$ a = first term, d = common diff, l = last term
Geometric sequence:	$u_n = ar^{n-1}$ $S_n = \frac{a(1-r^n)}{1-r} = \frac{a(1-r^n)}{r-1}, r \neq 1$ where a = first term, r = common ratio

Differentiation (IGCSE only)	
Rule	$x^n \Rightarrow nx^{n-1}$ Remember: Constants go to 0
Turning/Stationary Points (Max/Min)	Solve $\frac{dy}{dx} = 0$
Proving whether Max/Min	Use knowledge of shape of graph $+x^2$ happy face min $-x^2$ sad face max $+x^3$ max on left, min on right $-x^3$ min on left, max on right